

# Intrinsic Birefringence in 157 nm Materials

John H. Burnett, Zachary H. Levine, and Eric I. Shirley  
National Institute of Standards and Technology  
Gaithersburg, Maryland

MIT Lincoln Laboratories, Carl Zeiss, and Corning, Inc.

Support from SEMATECH

# Birefringence in Cubic Crystals

## I. Stress-Induced Birefringence

grown-in or externally applied (mounts, gravity, etc.)

- variable magnitude and orientation (sample-to-sample and within sample)
- weak dispersion visible-UV (NIST-SEMATECH 157 Review 11/00)
- can in principle be reduced to any desired value

## II. Intrinsic Birefringence

due to symmetry breaking effect of finite  $q$  of photon at short  $\lambda$

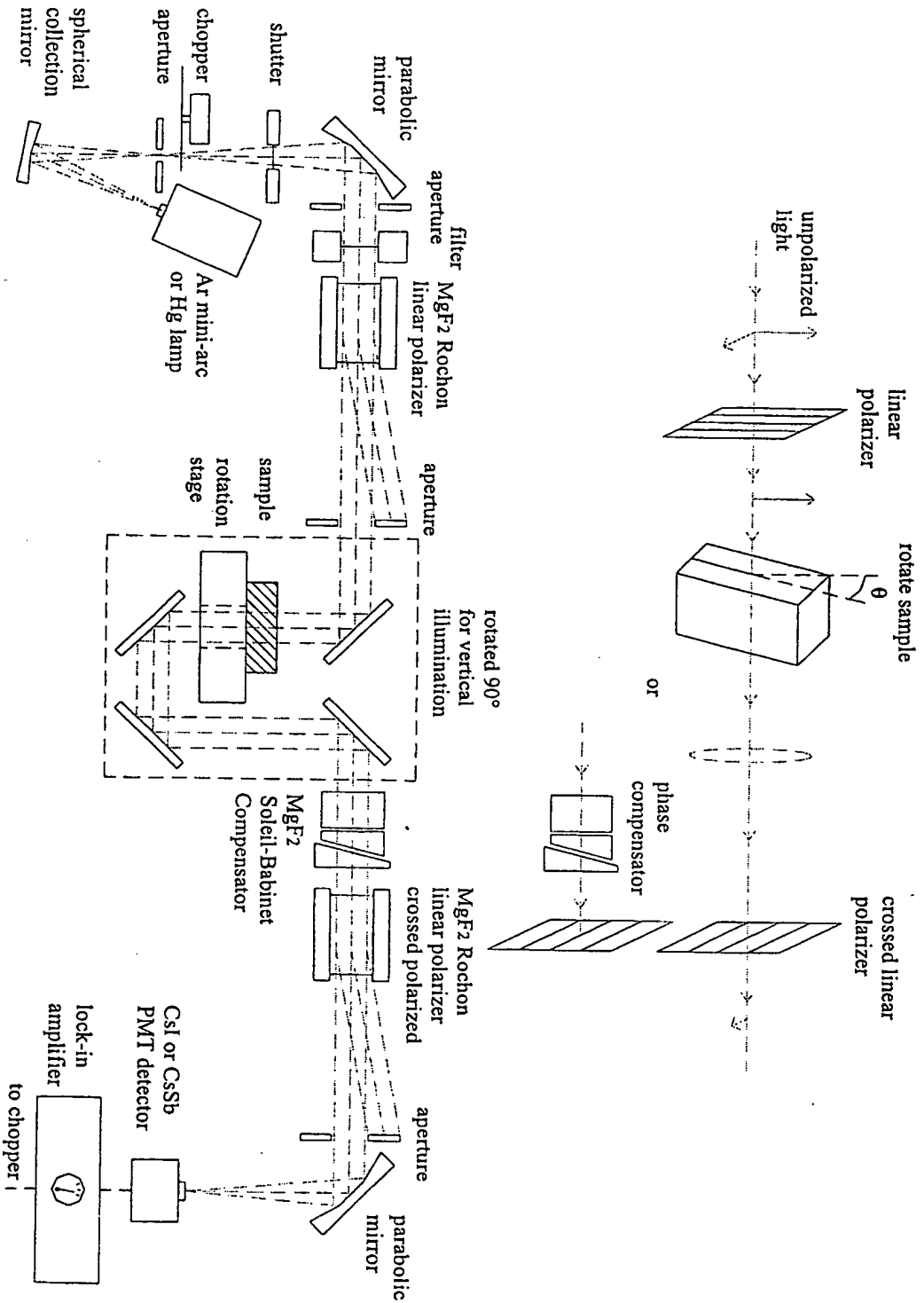
- preliminary measurements in  $\text{CaF}_2$  (above 157nm and 193nm target values)
- magnitude and orientation fixed by crystal (no sample dep., uniform)
- strong dispersion  $\sim 1/\lambda^2$
- CANNOT be reduced! (inherent property of crystal)

(but since fully predictable and symmetric, can be corrected for in principle)  
Has been measured in, e.g.,  $\text{Si}^1$  and  $\text{GaAs}^2$

<sup>1</sup>J. Pastnak and K. Vedam, Phys. Rev. B 3, 2567 (1971).

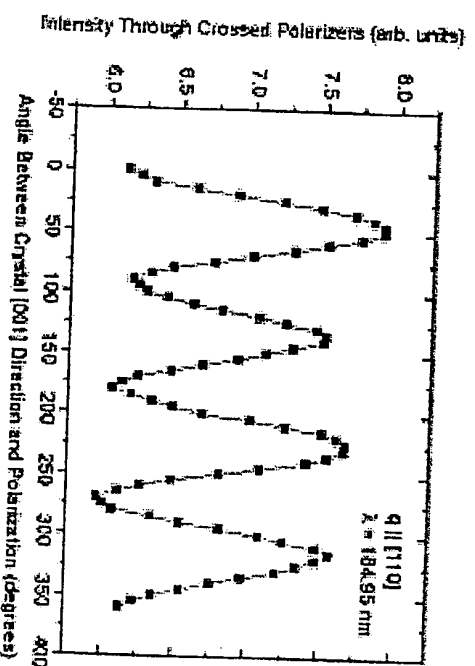
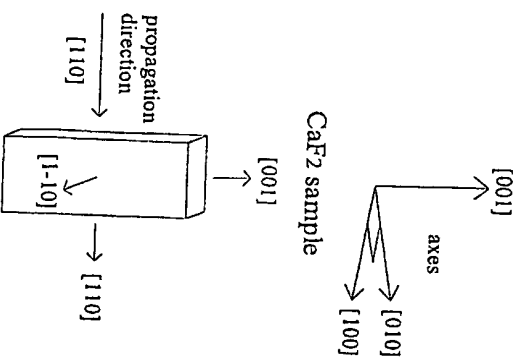
<sup>2</sup>P. Y. Yu and M. Cardona, Solid State Commun. 9, 1421 (1971).

# Birefringence Apparatus



# Birefringence Measurements at 185 nm

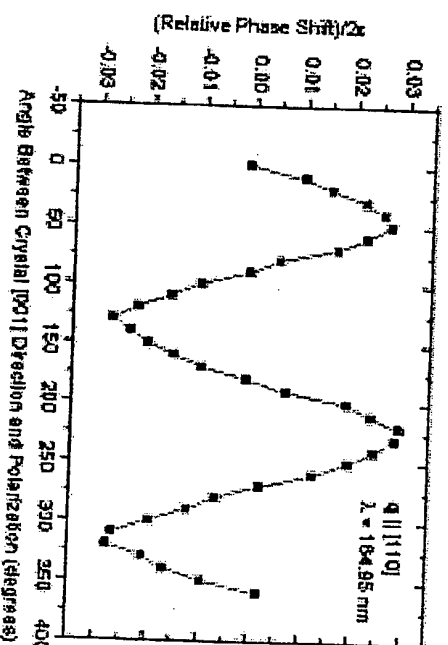
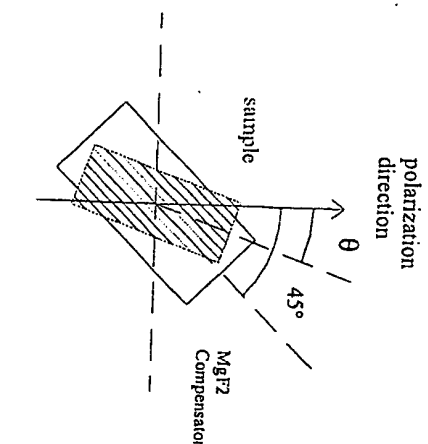
Conventional birefringence in meas. region @ 633nm <0.2 nm/cm



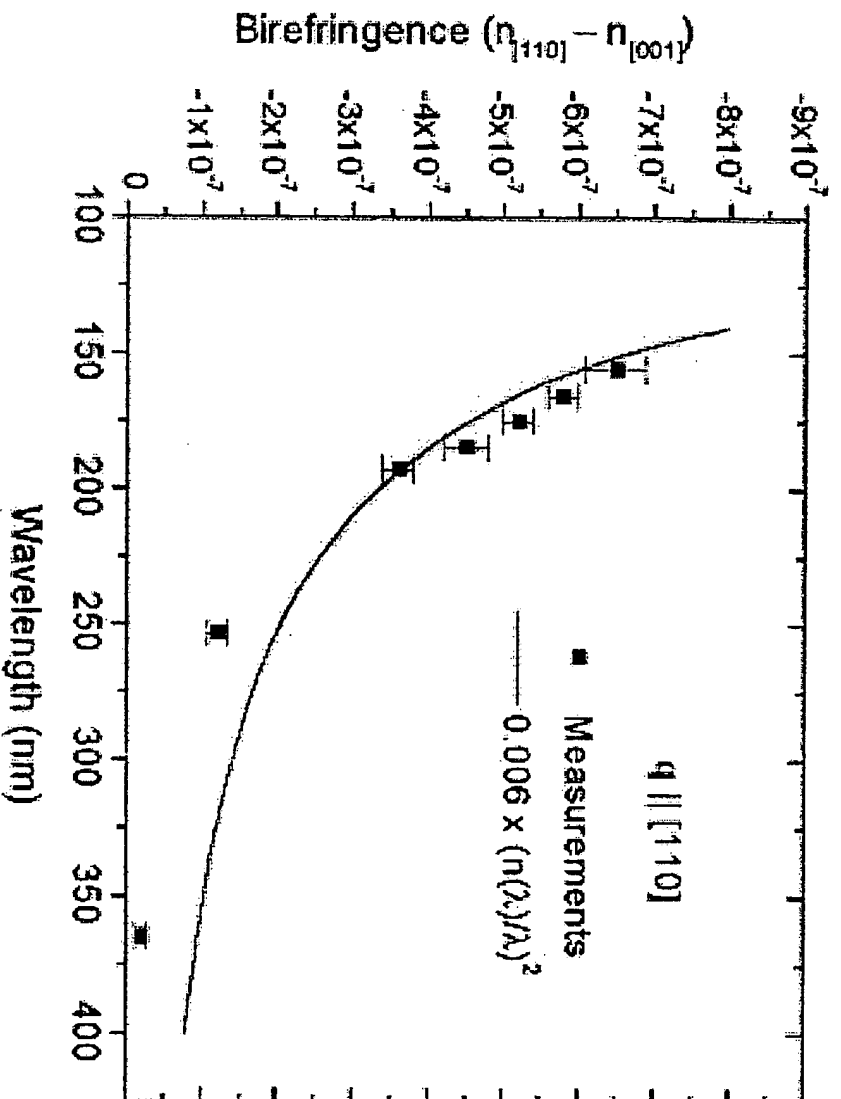
$$I/I_0 = \sin^2(\pi d \Delta n / \lambda) \sin^2(2\theta)$$

$$\Delta n = n_{[-110]} - n_{[001]}$$

$$\Delta n = (\lambda/d)(RPS/2\pi)$$



# Birefringence Results for $\text{CaF}_2$



Measurements of Birefringence of  $\text{CaF}_2$  in the UV

Wavelength (nm)	Line Source	$10^7 \times (n_{<110>} - n_{<001>})$
365.062	Hg I	$-0.19 \pm 0.08$
253.652	Hg I	$-1.2 \pm 0.1$
193.09	Cl	$-3.6 \pm 0.2$
184.95	Cl	$-4.5 \pm 0.3$
175.19	Cl	$-5.2 \pm 0.2$
165.72	Cl	$-5.8 \pm 0.2$
156.10	Cl	$-6.5 \pm 0.4$

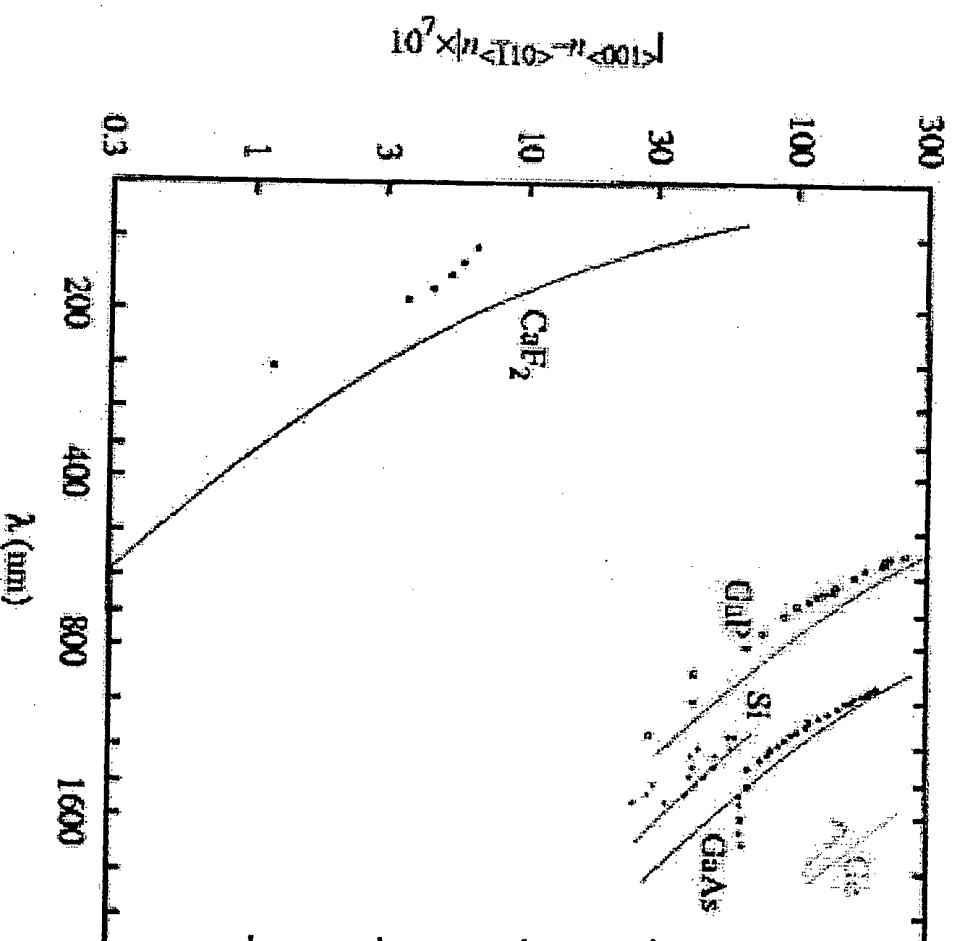
$$q \parallel [001] \rightarrow \Delta n = 0$$

$$q \parallel [111] \rightarrow \Delta n = 0$$

# First Principle Calculations

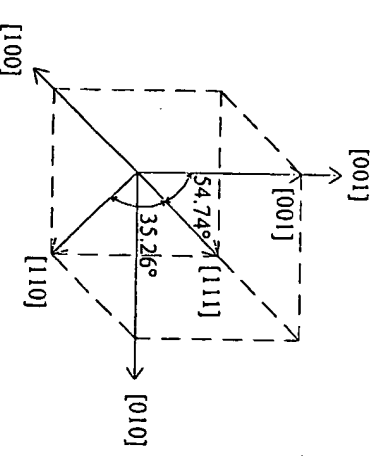
Takes only crystal structure and static dielectric const. from expt.

- for semiconductors,  $n_{<110>} - n_{<001>}$  positive in theory and expt. (meas. by others)
- for  $\text{CaF}_2$ ,  $n_{<110>} - n_{<001>}$  negative in theory and expt.



# Implications

- 1) Intrinsic birefringence  $\Delta n(157 \text{ nm}) \approx 6.5 \times 10^{-7}$  (6.5 nm/cm)
  - exceeds birefringence target value for 157 nm lithography (1 nm/cm) (1st Int. Symp. On 157 nm Lithography, May 2000)
- 2) Intrinsic birefringence  $\Delta n(193 \text{ nm}) = 3.6 \times 10^{-7}$  (3.6 nm/cm)
  - may exceed birefringence requirements of 193 nm lithography
- 3)  $\Delta n = 0$  for  $[111]$  direction (lens orientation)
  - but  $[110]$  only  $\theta = \cos^{-1}(2/3)^{1/2} = 35.26^\circ$  away
  - concern for high NA systems
- 4) Good news: effect completely predictable and symmetric
  - thus can correct for in principle
- 5) Need to know the full angle dependence of the effect
  - fortunately this is completely determined by symmetry alone



# Why Birefringence in Cubic Crystals?

Cubic crystals isotropic if **D** *linearly* related to **E** by 2nd rank tensor

$$D_i = \epsilon_{ij} E_j \quad (\epsilon_{ij} \text{ dielectric constant}) - \text{but assumes } \lambda \text{ large}$$

Actually  $\mathbf{D} = \mathbf{D}_0 e^{i\mathbf{q} \cdot \mathbf{r}} = \mathbf{D}_0 (1 + i\mathbf{q} \cdot \mathbf{r} - (\mathbf{q} \cdot \mathbf{r})^2/2 + \dots)$  ( $q = n2\pi/\lambda$ )  
(linear term doesn't contribute by symmetry)

$$\epsilon_{ij}(\mathbf{q}) = \epsilon(0)\delta_{ij} + \sum_{ijkl} \alpha_{ijkl} q_k q_l$$

Birefringence determined by fourth rank tensor  $\alpha_{ijkl} \propto (n/\lambda)^2$

Symmetry seen by  $(\mathbf{q} \cdot \mathbf{r})^2$  term - has azimuthal symmetry about **q**  
acts like uniaxial stress in direction of **q**

For crystal axes with 3-fold or 4-fold symmetry

effect of  $(\mathbf{q} \cdot \mathbf{r})^2$  term is to reduce isotropic to uniaxial

NO birefringence for  $\mathbf{q} \parallel \langle 111 \rangle$  or  $\mathbf{q} \parallel \langle 001 \rangle$

For all other directions  $(\mathbf{q} \cdot \mathbf{r})^2$  term results in biaxial birefringence

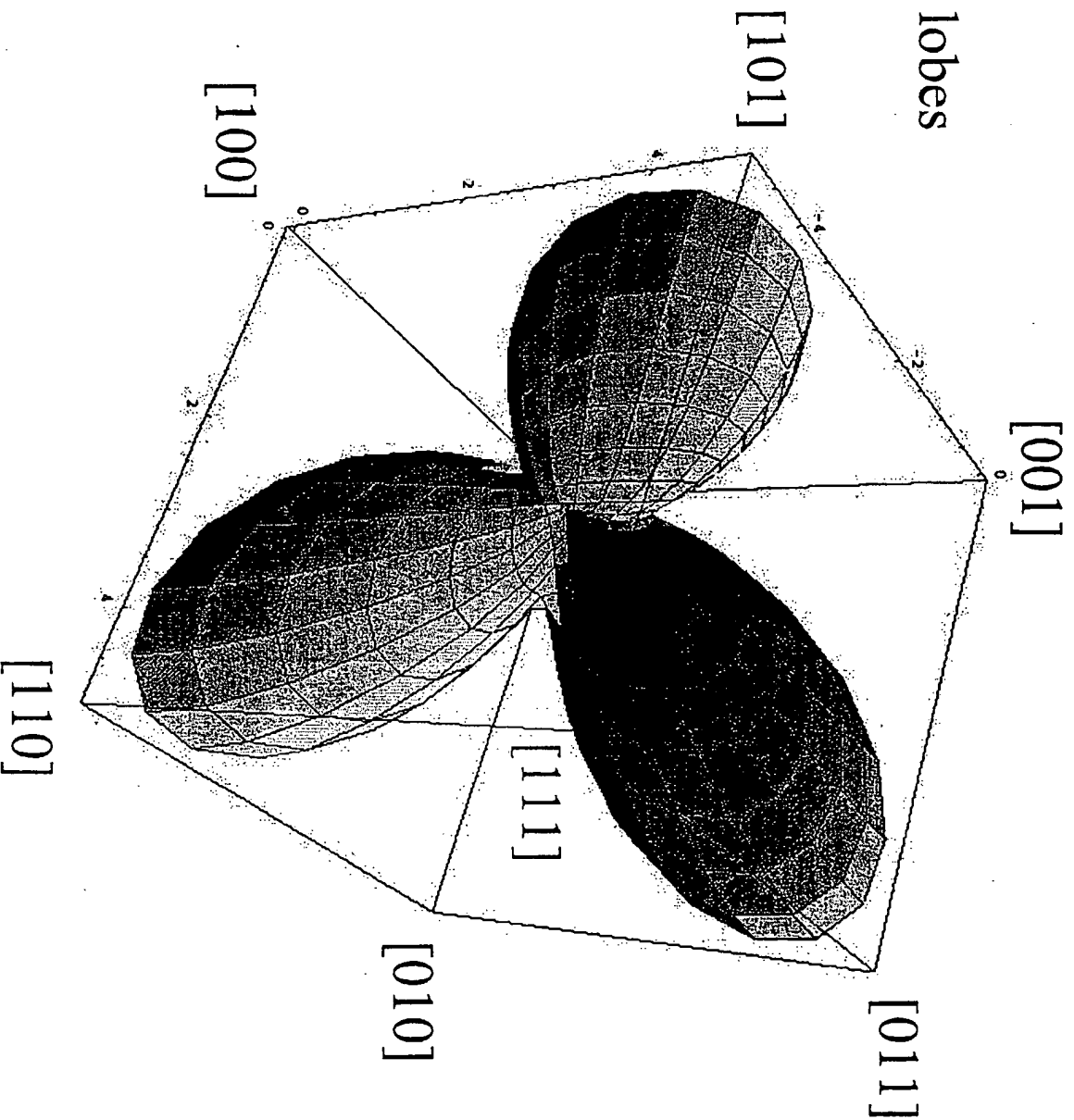
Further, symmetry breaking component  $\alpha$  has only one free parameter  
angle dependence determined by  $n_{\langle 110 \rangle} - n_{\langle 001 \rangle}$  alone!



# Intrinsic Birefringence

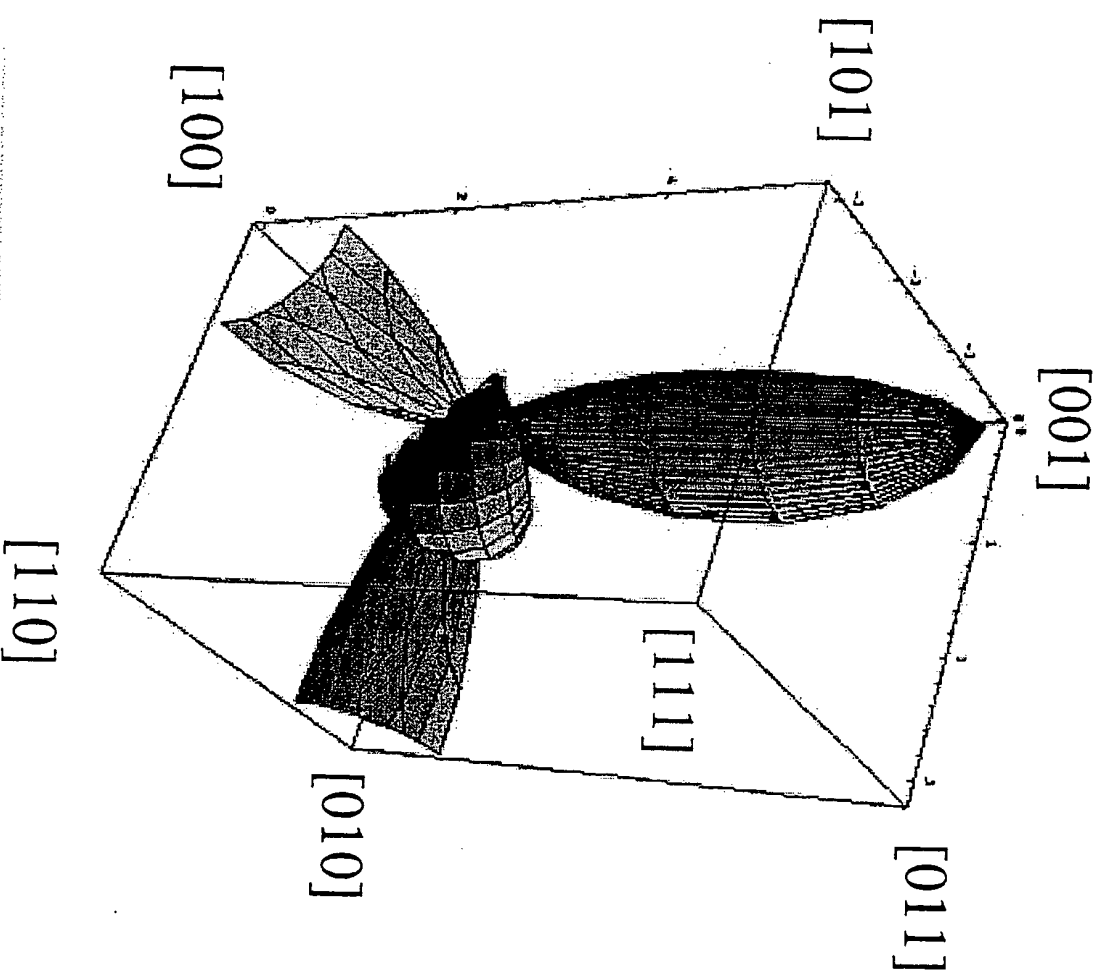
One octant - scaled according to  $\Delta n = 6.5 \times 10^{-7}$  for  $\mathbf{q} \parallel [110]$

Has 12 lobes



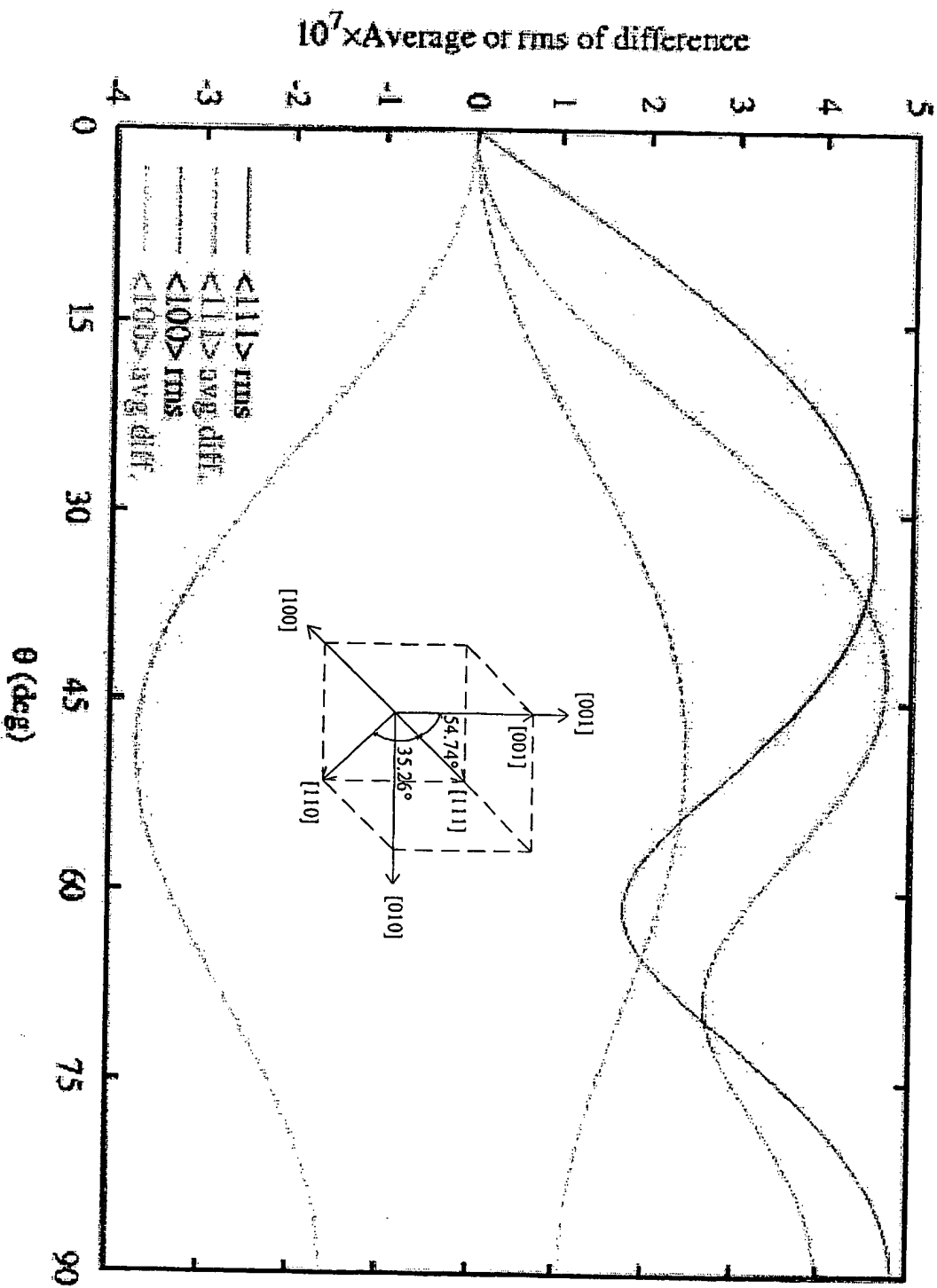
## Average Index Variation

One octant - scaled according to  $\Delta n = 6.5 \times 10^{-7}$  for  $\mathbf{q} \parallel [110]$



# Index Anisotropy

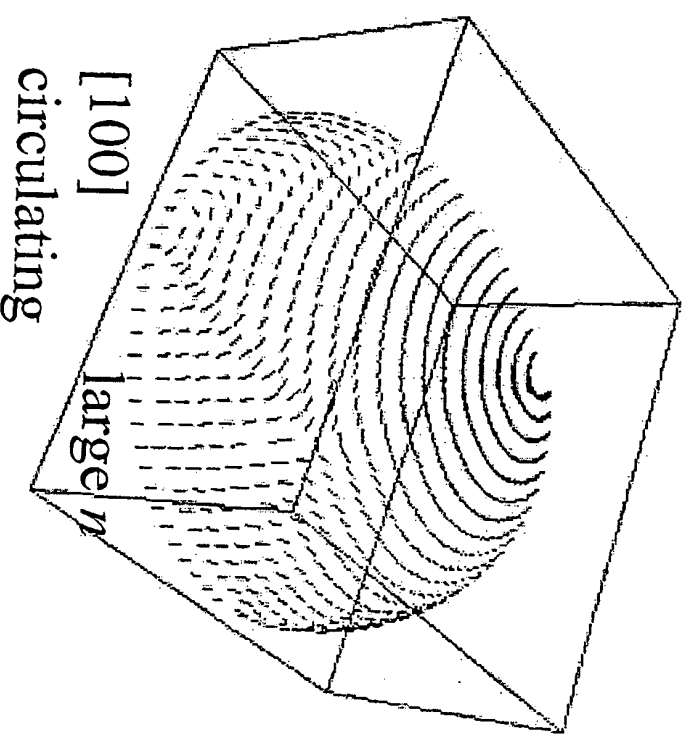
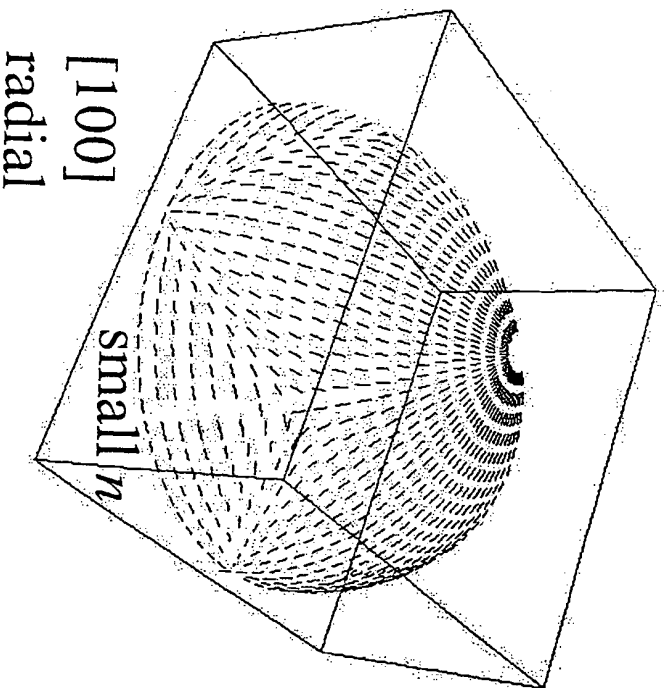
Azimuthal average - scaled according to  $\Delta n = 6.5 \times 10^{-7}$  for  $q \parallel [110]$



$\theta$  is deviation from indicated direction

## Eigenvector Directions

Shows directions of the two axes of birefringence plotted as a function of propagation direction represented as a point on a sphere. (magnitudes not indicated)



Detailed prescription for full solution available on request

# Conclusions

In Summary:

- 1) There **must** be intrinsic birefringence in  $\text{CaF}_2$  (and all cubics)
- 2) We have calculated the effect
- 3) Have measured the effect

$\Delta n = 0$  for  $q \parallel \langle 111 \rangle$  and  $q \parallel \langle 001 \rangle$ , as expected by symmetry  
max. value for  $q \parallel \langle 110 \rangle$ ,  $\Delta n(157\text{nm}) \approx 6.5 \times 10^{-7}$  (6.5 nm/cm)  
exceeds target value for 157nm (and for 193 nm?) High NA!

- 4) CANNOT be reduced! Intrinsic to material

measurements under way for other materials, e.g.,  $\text{BaF}_2$  and  $\text{LiF}$

- 5) Must live with it!

But, fully predictable and highly symmetric can correct for it  
e.g., pair [111] lenses with transverse axes rotated by  $60^\circ$

